

# Geometry-Aware Learning of Maps for Camera Localization

Samarth Brahmbhatt<sup>1</sup> Jinwei Gu<sup>2</sup> Kihwan Kim<sup>2</sup> James Hays<sup>1</sup> Jan Kautz<sup>2</sup>

<sup>1</sup>{samarth.robbo, hays}@gatech.edu <sup>2</sup>{jinweig, kihwank, jkautz}@nvidia.com

<sup>1</sup>Georgia Institute of Technology <sup>2</sup>NVIDIA

## Abstract

Maps are a key component in image-based camera localization and visual SLAM systems: they are used to establish geometric constraints between images, correct drift in relative pose estimation, and relocalize cameras after lost tracking. The exact definitions of maps, however, are often application-specific and hand-crafted for different scenarios (e.g. 3D landmarks, lines, planes, bags of visual words). We propose to represent maps as a deep neural net called MapNet, which enables learning a data-driven map representation. Unlike prior work on learning maps, MapNet exploits cheap and ubiquitous sensory inputs like visual odometry and GPS in addition to images and fuses them together for camera localization. Geometric constraints expressed by these inputs, which have traditionally been used in bundle adjustment or pose-graph optimization, are formulated as loss terms in MapNet training and also used during inference. In addition to directly improving localization accuracy, this allows us to update the MapNet (i.e., maps) in a self-supervised manner using additional unlabeled video sequences from the scene. We also propose a novel parameterization for camera rotation which is better suited for deep-learning based camera pose regression. Experimental results on both the indoor 7-Scenes dataset and the outdoor Oxford RobotCar dataset show significant performance improvement over prior work. The MapNet project webpage is <https://goo.gl/mRB3Au>.

## 1. Introduction

Camera localization *i.e.* recovering the 3D position and orientation of a moving camera is one of the fundamental tasks in computer vision with a wide variety of applications in robotics, autonomous driving, and AR/VR. A key component in camera localization, including various visual SLAM systems [20, 42, 56] and image-based localization methods [35, 46, 47] is the concept of a *map*. A map is an abstract summary of the input data that establishes geometric constraints between observations and can be queried to get the camera pose when tracking is drifting or lost. Maps, however, are usually defined in an application-specific man-

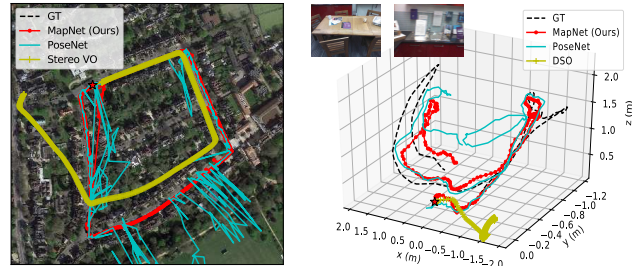


Figure 1: Camera localization results for outdoor (left) and indoor (right) scenes from the Oxford RobotCar [38] and 7-Scenes [48] datasets. As shown, prior DNN-based methods (e.g., PoseNet [32, 30, 31]) result in noisy estimations, while traditional visual odometry based methods (e.g., stereo VO or DSO [18]) often drift over time. In contrast, MapNet gives accurate camera pose estimates by including various geometric constraints in DNN training and inference.

ner with hand-crafted features. Examples include 3D landmarks for general visual SLAM methods [34, 35, 42], 3D lines and patches in semi-dense SLAM methods and indoor scenes [20, 43, 56], object-level context in semantic SLAM methods [10, 45], bag of visual word features on key frames for camera relocalization [12, 46, 47]. Being application-specific, these map representations may ignore useful (sometimes, the only available) features in environments they were not designed for, and are inflexible to update as more input data come in.

Is there a general map representation for camera localization that addresses these drawbacks? In this paper, we take a step towards answering this question. We propose to represent maps as a DNN, called MapNet, which learns the map representation directly from input data, with the flexibility to fuse multiple sensory inputs and to improve over time using unlabeled data. MapNet aims to be a part that can be easily plugged into any visual SLAM or image-based localization systems. We are inspired by both the recent DNN-based camera localization work (e.g., PoseNet [32] and its variants [11, 31, 40, 55]) in the context of structure-from-motion, as well as the traditional map optimization methods (e.g., bundle adjustment (BA) [22, 23, 39], pose graph optimization (PGO) [8, 17, 37]) in the context of visual SLAM. Compared to these prior works, our approach makes the fol-

lowing contributions:

- Most prior DNNs for camera localization [32, 30, 31, 11, 40, 55] are trained using single images labelled with absolute camera pose. In MapNet we show how the geometric constraints between pairs of observations can be included as an additional loss term in training. These constraints can come from a variety of sources: pose constraint from the visual odometry (VO) between pairs of images, translation constraint from two GPS readings, rotation constraint from two IMU readings, *etc.* We call this *geometry-aware learning* and show that it significantly improves camera localization performance in Section 4.
- PoseNet and its variants are *offline* methods – the learned DNNs are fixed after training. In contrast, we propose MapNet+ that can use the geometric constraints between pairs of observations mentioned above to continuously update the DNN weights (*i.e.*, maps) without absolute camera pose supervision, as additional unlabeled data come in. Moreover, at run-time, we also exploit the complementary noise characteristics of MapNet predictions (locally noisy but drift-free) and VO (locally smooth but drift-y) by fusing them in a moving window fashion with PGO. We call this variant MapNet+PGO. We show in Section 4 that both MapNet+ and MapNet+PGO successively improve performance further.
- We propose a new parameterization for camera rotation, the logarithm of unit quaternion, which is better suited for deep-learning based camera pose regression. This improves the performance of PoseNet and MapNet, as shown in Table 2.

Figure 1 shows two examples of camera localization. Pure DNN-based methods (*e.g.*, PoseNet [32, 30, 31]) result in noisy estimations, and the traditional VO-based methods (*e.g.*, stereo VO or DSO [18]) often drift significantly over time. By incorporating the geometric constraints into DNN-based learning and inference, the proposed approach MapNet+PGO achieves the best result. We evaluate the proposed methods extensively on both the indoor 7-Scenes [48] and the outdoor Oxford RobotCar dataset [38].

## 2. Related Work

### Maps in Visual SLAM and Image-based Localization

Over the years, various types of map representations and their optimization techniques have been proposed for camera localization [52, 54]. In visual SLAM, 3D landmarks (with feature descriptors of the corresponding image patches) are often defined as maps in both Bayesian filtering approaches [14, 41, 53] and key-frame based approaches [34, 42, 49]. The features are often modeled in

various forms such as points [14, 34], points and lines [21], points and planes [51], or built on more semantic (object) level features [10, 45]. However, the choice of the representation has been application-specific, and thus the performance can vary depending on a target scene (*i.e.*, amount of lines, planes or texture present in the scene). To address this issue, recently, direct [27, 43] and semi-direct methods [18, 20] utilize all the pixels with high gradients rather than features to build maps. While they provide more stable pose estimate and denser information of a scene, they require a higher computational expense, and often need an accurate intrinsic calibration and initialization because they are sensitive to photometric consistency [5].

For map optimization, since Lu and Milios [37] first introduced a graph-based method to refine a map with global optimization of local nodes (measurements from odometry), various types of these local-to-global pose graph optimization methods have been proposed [15, 24, 52, 53]. Similarly, bundle adjustment [36, 54] has also been a popular choice for methods using structure from motion techniques (*i.e.*, keyframe-based approaches) [34, 42, 49].

In the context of image-based localization, visual place recognition [46, 47, 35] and camera relocalization [42], image descriptors (*e.g.*, bag-of-words (BoW) features [12], VLAD [4], Fisher vectors [28], and recent DNN-based features [3]) are used to build maps/vocabularies for image retrieval and pose estimation.

Compared to these prior application-specific map definitions, in this paper we primarily focus on learning a general map representation for sequential camera localization with deep neural networks, by leveraging statistical learning from big data and geometric constraints from pose graph optimization and bundle adjustment.

**DNN-based Camera Localization** A few recent works use deep neural networks for image-based localization in the context of structure-from-motion. PoseNet [32] first proposed to directly regress 6-DoF camera pose from an input image with GoogLeNet. Kendall *et al.* [30, 31] extend PoseNet by learning the weight between camera translation and rotation loss and incorporating the reprojection loss. Melekhov *et al.* [40] improved PoseNet with skip connections with ResNet34 architecture. Brachmann *et al.* [7] localize a camera in a dense 3D reconstruction by performing RANSAC on predicted 2D-3D correspondences. Recently, RNNs (*e.g.*, LSTM) have been introduced to spatially [55] and temporally [11] improve camera localization.

MapNet is inspired by the PoseNet line of work, but has several major modifications. Table 1 shows a comparative summary. Clark *et al.* [11] used an LSTM to implicitly learn the temporal relationship between consecutive frames, but its performance is on-par or worse than prior methods [31, 40]. In contrast, MapNet uses single images as input during inference but still uses the geometric con-

Table 1: Comparison with prior DNN-based camera localization methods. Please refer to Section 2 for details.

	PoseNet [32, 30, 31]	Hourglass [40]	LSTM-Pose [55]	VidLoc [11]	(Proposed)		
					MapNet	MapNet+	MapNet+PGO
Input	Images	Images	Images	Videos	Images	unlabeled videos + (VO, GPS, IMU)	
Fusion ability	No	No	No	No	No	Yes	Yes
Self-supervised update	No	No	No	No	No	Yes	No
Temporal constraint	No	No	No	Yes	Yes	Yes	Yes
Geometry aware	Reprojection [31]	No	No	No	Geometric constraints on camera poses		

straints between pairs as a meaningful learning signal for training. MapNet+ and MapNet+PGO use unlabeled videos and multiple sensory input (*e.g.*, visual odometry, IMU, GPS) to further improve performance. Thus, they can fuse information from multiple modalities and improve in a self-supervised manner. In [31] Kendall *et al.* make PoseNet *scene-geometry* aware by minimizing the reprojection error of 3D points in multiple images. In contrast, MapNet is *camera motion-geometry* aware by utilizing the geometric constraints between camera poses.

### 3. Proposed Approach

In this paper, we learn a general map representation for sequential camera localization with deep neural networks (DNNs). Maps are represented as learned weights of a DNN trained to regress camera pose. Figure 2 shows all of our three proposed models. At the heart of MapNet is a DNN that regresses absolute camera pose from an input image, which is described in detail in Section 3.1. MapNet takes in tuples of images and additionally enforces constraints between pose predictions for pairs, as described in Section 3.2. MapNet+ improves a trained MapNet by utilizing the geometric constraints expressed by visual odometry (VO) on additional unlabeled videos from the same scene, or synchronized GPS readings (Section 3.3). Finally, we employ moving-window PGO during inference to obtain a smooth and drift free camera trajectory by fusing MapNet+ absolute pose predictions and VO (Section 3.4).

#### 3.1. Camera Pose Regression with DNNs

Our work is built upon prior works in DNN-based pose estimation methods [11, 30, 31, 32, 40, 55], which regress 6-DoF camera pose from an input RGB image with a DNN. In our work, we made several modifications to PoseNet [31, 32]. First, we use ResNet-34 [25] and modify it by introducing a global average pooling layer after the last conv layer, followed by a fc layer with 2048 neurons, a ReLU and dropout with  $p = 0.5$ . This is followed by a final fc layer that outputs a 6-DoF camera pose.

Second, we propose to parameterize camera orientation as the logarithm of a unit quaternion [2], which is better suited for regression with deep learning. PoseNet and its variants [11, 31, 32, 40, 55] used 4-d unit quaternions to

represent orientation, and regress it with  $l_1$  or  $l_2$  norm. This has two issues: (1) the quadruple is an over parameterization of the 3-DoF rotation, and (2) normalization of the output quadruple is required but often results in worse performance [32, 31, 40]. While Euler angles used in [50] are not over-parameterized, they are not suited for regression since they wrap around  $2\pi$ .

The logarithm of a unit quaternion,  $\log \mathbf{q}$  has 3 dimensions and is not over-parameterized. This allows us to directly use the  $l_1$  or  $l_2$  distance as the loss function without normalization. The logarithm of a unit quaternion  $\mathbf{q} = (u, \mathbf{v})$ , where  $u$  is a scalar and  $\mathbf{v}$  is a 3-d vector, is defined as [13, 29]

$$\log \mathbf{q} = \begin{cases} \frac{\mathbf{v}}{\|\mathbf{v}\|} \cos^{-1} u, & \text{if } \|\mathbf{v}\| \neq 0 \\ \mathbf{0}, & \text{otherwise} \end{cases} \quad (1)$$

The logarithmic form  $\mathbf{w} = \log \mathbf{q}$  can be converted back to a unit quaternion by the formula  $\exp \mathbf{w} = (\cos \|\mathbf{w}\|, \frac{\mathbf{w}}{\|\mathbf{w}\|} \sin \|\mathbf{w}\|)$ . As shown in Table 2 in Section 4, using this rotation parameteration achieve better results than PoseNet [31]. We also implemented other metrics for rotation [26], and found they did not improve the performance.

#### 3.2. MapNet: Geometry-Aware Learning

Similar to PoseNet [11, 31, 32, 40, 55], MapNet also learns a DNN  $\Theta$  that estimates the 6-DoF camera pose  $\mathbf{p} = (\mathbf{t}, \mathbf{w})$  from an input RGB image  $\mathbf{I}$  on the training set  $\mathcal{D} = \{(\mathbf{I}, \mathbf{p}^*)\}$  via supervised learning,  $f(\mathbf{I}; \Theta) = \mathbf{p}$ . The main difference, however, is that MapNet minimizes both the loss of the per-image absolute pose and the loss of the relative pose between image pairs, as shown in Fig. 2,

$$L_{\mathcal{D}}(\Theta) = \sum_{i=1}^{|\mathcal{D}|} h(\mathbf{p}_i, \mathbf{p}_i^*) + \alpha \sum_{i,j=1, i \neq j}^{|\mathcal{D}|} h(\mathbf{v}_{ij}, \mathbf{v}_{ij}^*), \quad (2)$$

where  $\mathbf{v}_{ij} = (\mathbf{t}_i - \mathbf{t}_j, \mathbf{w}_i - \mathbf{w}_j)$  is the relative camera pose between pose predictions  $\mathbf{p}_i$  and  $\mathbf{p}_j$  for images  $\mathbf{I}_i$  and  $\mathbf{I}_j$ .  $h(\cdot)$  is a function to measure the distance between the predicted camera pose  $\mathbf{p}$  and the ground truth camera pose  $\mathbf{p}^*$ , defined as [31]:

$$h(\mathbf{p}, \mathbf{p}^*) = \|\mathbf{t} - \mathbf{t}^*\|_1 e^{-\beta} + \beta + \|\mathbf{w} - \mathbf{w}^*\|_1 e^{-\gamma} + \gamma, \quad (3)$$

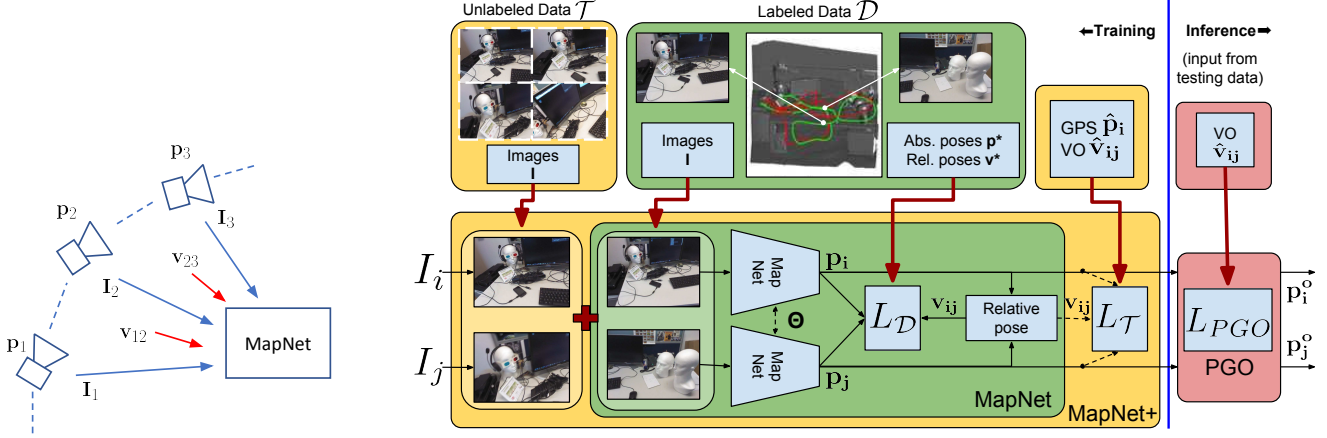


Figure 2: **Left:** MapNet learns a general map representation directly from input data, including images, visual odometry (VO), and other sensory inputs. **Right:** Data flow for our proposed algorithms. MapNet enforces geometric constraints between relative poses and absolute poses in network training. MapNet+ fuses other inputs such as visual odometry to update maps with self-supervised learning. MapNet+PGO performs PGO at testing time to further improve accuracy.

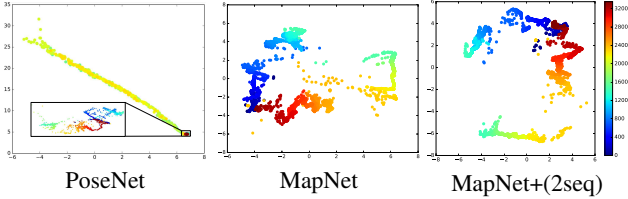


Figure 3: 2D multi-dimensional scaling (MDS) of penultimate layer features for various models trained on the LOOP sequence from Oxford RobotCar [38]. Input images are from a held-out test sequence (see Fig. 1 for ground-truth camera poses). The points are chronologically colored. Features learned by PoseNet do not correlate with the distribution of ground truth camera poses, while those learned by MapNet and MapNet+ show successively better correlation with the ground truth camera poses (see Fig. 5).

where  $\beta$  and  $\gamma$  are the weights that balance the translation loss and rotation loss. Both  $\beta$  and  $\gamma$  are learned during training with initialization  $\beta_0$  and  $\gamma_0$ .  $(I_i, I_j)$  are image pairs within each tuple of  $s$  images sampled with a gap of  $k$  frames from  $\mathcal{D}$ . Intuitively, adding the second loss of the relative camera poses between image pairs helps to enforce global consistency, which improves the performance of camera localization (see Section. 4).

To understand more about the representation MapNet learns, we visualize the distribution of the feature vectors of the last activation layer using 2D multi-dimensional scaling (MDS) [6]. We chose MDS rather than T-SNE because it is designed to preserve global structure of the feature space. In Fig. 3, we show that PoseNet [31] feature vectors for test images captured along a loop in the Oxford RobotCar dataset [38] do not correlate with the distribution of ground truth camera poses, while the features learned by MapNet and MapNet+ (next subsection) show successively better correlation. All models use the same network architecture.

### 3.3. MapNet+: Update with Unlabeled Data

Both PoseNet and MapNet require labelled data (*i.e.*, images with absolute camera poses) to train. In many real applications, we may also have lots of unlabeled data, *e.g.*, videos captured at different times or camera motions in the same scene. Off-the-shelf VO algorithms [18, 19] provide relative camera poses between image pairs from these videos. Other sensors (*e.g.*, IMU and GPS) can also provide measurements about camera pose, especially for challenging conditions (*e.g.*, textureless, low-light). MapNet+ fuses these additional data  $\mathcal{T}$  to update the weights of MapNet with self-supervised learning.

Suppose the additional data are some videos of the same scene,  $\mathcal{T} = \{I_t\}$ . We can compute the relative poses  $\hat{v}_{ij}$  between consecutive frames with visual odometry algorithms [18, 19, 44]. In order to update the map with  $\mathcal{T}$ , we fine-tune a pre-trained MapNet  $\Theta$  by minimizing a loss function that consists of the original loss from the labelled dataset  $\mathcal{D}$  and the loss from the unlabeled data  $\mathcal{T}$ ,

$$L(\Theta) = L_{\mathcal{D}}(\Theta) + L_{\mathcal{T}}(\Theta), \quad (4)$$

where  $L_{\mathcal{T}}(\Theta)$  is the distance between the relative camera pose  $v_{ij}$  (from predictions  $p_i, p_j$ ) and visual odometry  $\hat{v}_{ij}$ ,

$$L_{\mathcal{T}}(\Theta) = \sum_{i,j=1, i \neq j}^{|\mathcal{T}|} h(v_{ij}, \hat{v}_{ij}) \quad (5)$$

Since VO algorithms compute  $\hat{v}_{ij}$  in the coordinate system of camera  $i$ , the relative pose  $v_{ij}$  is also computed in that coordinate system:

$$v_{ij} = (\exp(\mathbf{w}_j)(\mathbf{t}_i - \mathbf{t}_j)\exp(\mathbf{w}_j)^{-1}, \log(\exp(\mathbf{w}_j)^{-1}\exp(\mathbf{w}_i))), \quad (6)$$



Note that we still keep the supervision loss  $L_{\mathcal{D}}(\Theta)$  from  $\mathcal{D}$  — this is important to avoid trivial solutions if we optimize only the self-supervised loss  $L_{\mathcal{T}}(\Theta)$  from  $\mathcal{T}$ . Thus each mini-batch samples half from the labelled data  $\mathcal{D}$  and half from the unlabeled data  $\mathcal{T}$ . The image pairs  $(\mathbf{I}_i, \mathbf{I}_j)$  are sampled similarly from tuples of  $s$  images with a gap of  $k$  frames from both  $\mathcal{D}$  and  $\mathcal{T}$ .

Intuitively, MapNet+ exploits the complimentary characteristics of VO and DNN-based pose prediction — VO is locally accurate but often drifts over time, and DNN-based pose predictions are noisy but drift-free. For other sensors such as IMU (which measures relative rotation) and GPS (which measures 3D locations), we can define similar loss terms  $L_{\mathcal{T}}(\Theta)$  that minimize the difference between such measurements and the predictions from the MapNet.

### 3.4. MapNet+PGO: Optimizing During Inference

During inference, MapNet+PGO fuses the absolute pose predictions from MapNet+ and the relative poses from VO using pose graph optimization (PGO) [8, 37, 17] to get smooth and globally consistent pose predictions. It runs in a moving-window of  $T$  frames. Suppose the initial poses predicted by MapNet+ are  $\{\mathbf{p}_i\}_{i=1}^T$ , and the relative poses between two frames from VO are  $\{\hat{\mathbf{v}}_{ij}\}$  where  $i, j \in [1, T], i \neq j$ . MapNet+PGO solves for the optimal poses  $\{\mathbf{p}_i^o\}_{i=1}^T$  by minimizing the following cost:

$$L_{PGO}(\{\mathbf{p}_i^o\}_{i=1}^T) = \sum_{i=1}^T \bar{h}(\mathbf{p}_i^o, \mathbf{p}_i) + \sum_{i,j=1, i \neq j}^T \bar{h}(\mathbf{v}_{ij}^o, \hat{\mathbf{v}}_{ij}), \quad (7)$$

where  $\bar{h}(\cdot)$  is the standard pose distance function used in PGO literature [24]. PGO is an iterative algorithm where internally  $\mathbf{v}_{ij}^o$  is derived from  $\mathbf{p}_i^o$  and  $\mathbf{p}_j^o$  as in Equation (6). Details and derivation are included in the supplementary material. Note here we fix the DNN weights  $\Theta$  and only optimize  $\{\mathbf{p}_i^o\}_{i=1}^T$ . As shown in Section 4, MapNet+PGO further improves the accuracy of pose estimation, with a minimal extra computational cost at testing.

### 3.5. Implementation Details

We implemented our algorithms with PyTorch [1], using the Adam optimizer [33] with a learning rate of  $1e-4$  and a weight decay of  $5e-4$ . The input images are scaled to  $341 \times 256$  pixels, and normalized by pixel mean subtraction and standard deviation division. We set the weight coefficient  $\alpha = 1$  and initializations  $\beta_0 = 0.0$  and  $\gamma_0 = -3.0$ . Image pairs are sampled from tuples of size  $s = 3$  with spacing  $k = 10$  frames for MapNet and MapNet+, and  $T = 7$ ,  $k = 150$  frames for PGO.<sup>1</sup> All models are trained for 300 epochs, except for MapNet+, which is finetuned with  $\alpha = 0$  for 5 epochs from a trained MapNet.

<sup>1</sup>PGO for RobotCar sequences uses frame separation  $T = 7$ ,  $k = 10$ .

## 4. Experimental Evaluations

**Datasets** We evaluate our algorithms on two well-known public datasets — 7-Scenes [48] for small-scale, indoor, AR/VR-type scenarios, and Oxford RobotCar [38] for large-scale, outdoor, autonomous driving scenarios. 7-Scenes contains RGB-D image sequences of seven indoor environments (with the spatial extent less than 4 meters) captured with a Kinect sensor. Multiple sequences were captured for each environment, and each sequence is 500 or 1000 frames. The ground truth camera poses are obtained with KinectFusion. The 7-Scenes dataset has recently been evaluated extensively as a benchmark [32, 30, 31, 40, 55, 11, 7], which makes it ideal for us to compare with prior state-of-the-art methods.

Oxford RobotCar contains over 100 repetitions of a consistent route (about 10km) through central Oxford captured twice a week over a period of over a year. Thus the dataset captures different combinations of weather, traffic, pedestrians, construction and roadworks. In addition to the images captured with the six cameras mounted on the car, the dataset also contains LIDAR, GPS and INS measurements, as well as stereo visual odometry (VO). We extracted two subsets from this dataset: LOOP (Fig. 1) with a total length of 1120m, which was also used in VidLoc [11], and FULL (Fig. 6) with a total length of 9562m. Details of the training, validation, and testing sequences are provided in the supplementary material.

**Baselines and Data Augmentation** We compare our approach with two groups of prior methods on 7-Scenes. For the DNN-based prior work, we compare with PoseNet15 [32], PoseNet16 [30], PoseNet17 [31], Hourglass [40], LSTM-PoseNet [55], and VidLoc [11]. For the traditional visual odometry based methods, we used DSO [18] to compute the VO and integrate to obtain camera poses. We run the DSO with images at the same spatial resolution as MapNet. On Oxford RobotCar, only VidLoc [11] reported results on the LOOP scene but it did not provide training and testing sequences. Thus, the two baselines to compare are the provided stereo VO, as well as our version of PoseNet (with log q). In RobotCar, we randomly perturb the brightness, saturation, hue and contrast of images during training for experiments, which we found essential for performing cross-weather and cross-time localization.

### 4.1. Experiments on the 7-Scenes Dataset

**Effects of Rotation Parameterization** In Section 3.1, we introduced a new parameterization of camera orientation for PoseNet and used ResNet34 as the base network. Table 2 shows the quantitative results of these modifications to the baseline PoseNet. Following the same convention of prior work [32, 30, 31, 40, 55, 11], we compute the median error

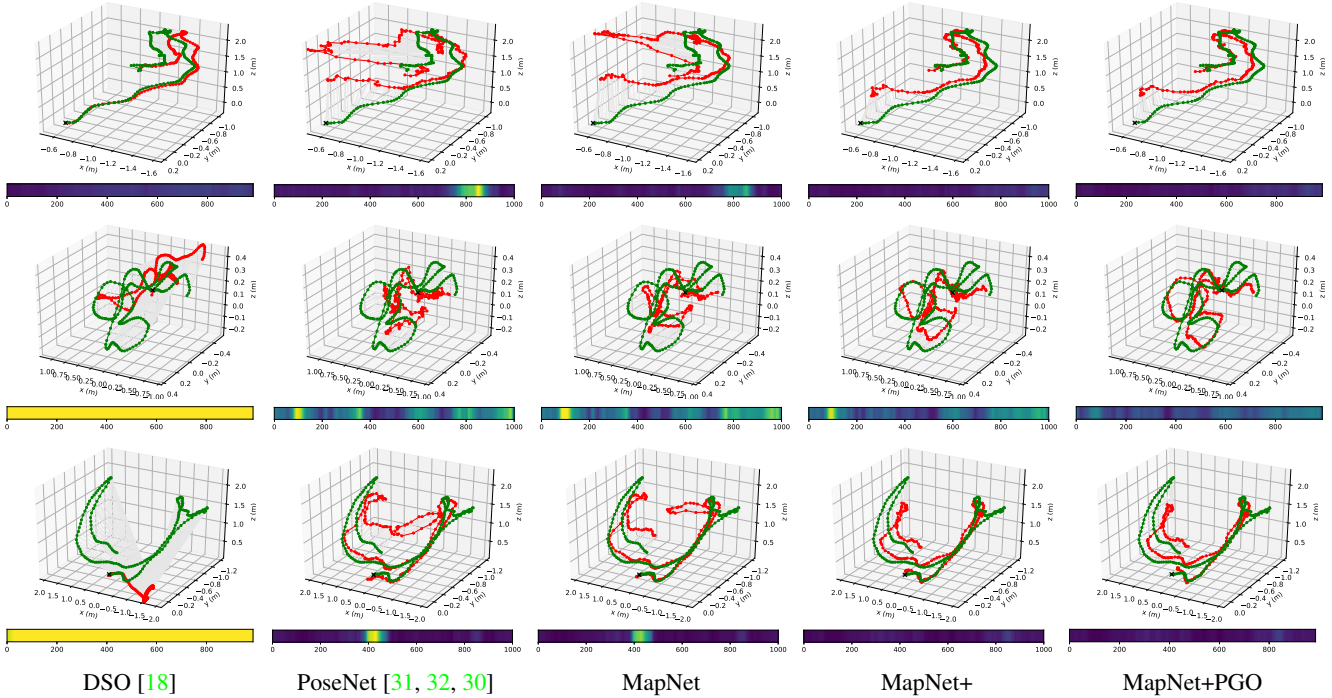


Figure 4: **Camera localization results on 7-Scenes dataset [48].** For each subfigure, the top 3D plot shows the camera trajectory (green for the ground truth and red for the prediction), and the bottom color bar shows rotation error for all the frames. From top to bottom, the three testing sequences are: Redkitchen-seq-03, Heads-seq-01, and Redkitchen-seq-12. See Table 3 for quantitative comparison.

Table 2: Translation and rotation error on the 7-Scenes dataset.

Scene	PoseNet17 [31]	PoseNet (ResNet34)	PoseNet+log $\mathbf{q}$ (ResNet34)
Chess	0.13m, 4.48°	<b>0.11m, 4.24°</b>	<b>0.11m, 4.29°</b>
Fire	<b>0.27m, 11.30°</b>	0.29m, 11.68°	<b>0.27m, 12.13°</b>
Heads	<b>0.17m, 13.00°</b>	0.20m, 13.11°	0.19m, <b>12.15°</b>
Office	<b>0.19m, 5.55°</b>	<b>0.19m, 6.40°</b>	<b>0.19m, 6.35°</b>
Pumpkin	0.26m, <b>4.75°</b>	0.23m, 5.77°	<b>0.22m, 5.05°</b>
Red Kitchen	<b>0.23m, 5.35°</b>	0.27m, 5.81°	0.25m, <b>5.27°</b>
Stairs	0.35m, 12.40°	0.31m, 12.43°	<b>0.30m, 11.29°</b>
Average	0.23m, 8.12°	0.23m, 8.49°	<b>0.22m, 8.07°</b>

for camera translation and rotation.<sup>2</sup> As shown, our proposed rotation parameterization does improve performance.

**Comparison with Prior Methods** Figure 4 shows the camera trajectories for several testing sequences from the 7-Scenes dataset for DSO VO, PoseNet, MapNet, MapNet+, and MapNet+PGO. Table 3 shows quantitative comparisons. The unlabeled data used to fine-tune MapNet+ for these experiments are the unlabeled test sequences. This is a transductive learning scenario [9, 16]. As shown, DSO often drifts over time and PoseNet results in noisy predictions. In contrast, by including various geometric constraints into network training and inference our proposed approaches MapNet, MapNet+ and MapNet+PGO suc-

<sup>2</sup>Other statistics of the camera pose estimation errors are also provided in the supplementary material, which support the same conclusion.

sively improve the performance. A complete table for all testing sequences from the 7-Scenes dataset is included in the supplementary material.

## 4.2. Experiments on the Oxford RobotCar Dataset

**Results on the LOOP Route** We first train a baseline PoseNet (with the log  $\mathbf{q}$  parameterization for rotation) and a MapNet model using two labelled sequences captured on the LOOP route under cloudy weather, while the testing sequence is captured under sunny weather. We then perform two experiments with different auxiliary data for MapNet+.

In the first experiment, MapNet+ is trained on additional unlabeled LOOP sequences separate from the testing sequence, with stereo VO provided with the dataset. To tease apart the influence of labeled and unlabeled data in the effectiveness of our MapNet+ models, we train them with varying amounts of labeled (one to two sequences) and unlabeled data (zero to three sequences). Figure 8 shows the mean translation and rotation errors of these models on the testing sequence. While labeled data is clearly more important than an equal amount of unlabeled data, we show that unlabeled data does consistently improve performance as more becomes available. This trend bodes well for real-world scenarios, where the amount of unlabeled data available far exceeds the amount of labeled data.

In the second experiment, MapNet+ is trained with GPS *i.e.*, the dataset  $\mathcal{T}$  contains two sequences of images and

Table 3: Translation error (m) and rotation error ( $^{\circ}$ ) for various methods on the 7-Scenes dataset [48].

Scene	PoseNet17 [31]	Hourglass [40]	LSTM-Pose [55]	VidLoc [11]	DSO [18]	MapNet	MapNet+	MapNet+PGO
Chess	0.13m, 4.48 $^{\circ}$	0.15m, 6.17 $^{\circ}$	0.24m, 5.77 $^{\circ}$	0.18m, NA	0.17m, 8.13 $^{\circ}$	<b>0.08m</b> , 3.25 $^{\circ}$	0.10m, <b>3.17<math>^{\circ}</math></b>	0.09m, 3.24 $^{\circ}$
Fire	0.27m, 11.30 $^{\circ}$	0.27m, 10.84 $^{\circ}$	0.34m, 11.9 $^{\circ}$	0.26m, NA	<b>0.19m</b> , 65.0 $^{\circ}$	0.27m, 11.69 $^{\circ}$	0.20m, <b>9.04<math>^{\circ}</math></b>	0.20m, 9.29 $^{\circ}$
Heads	0.17m, 13.00 $^{\circ}$	0.19m, 11.63 $^{\circ}$	0.21m, 13.7 $^{\circ}$	0.14m, NA	0.61m, 68.2 $^{\circ}$	0.18m, 13.25 $^{\circ}$	0.13m, 11.13 $^{\circ}$	<b>0.12m</b> , <b>8.45<math>^{\circ}</math></b>
Office	0.19m, 5.55 $^{\circ}$	0.21m, 8.48 $^{\circ}$	0.30m, 8.08 $^{\circ}$	0.26m, NA	1.51m, 16.8 $^{\circ}$	<b>0.17m</b> , <b>5.15<math>^{\circ}</math></b>	0.18m, 5.38 $^{\circ}$	0.19m, 5.42 $^{\circ}$
Pumpkin	0.26m, 4.75 $^{\circ}$	0.25m, 7.01 $^{\circ}$	0.33m, 7.00 $^{\circ}$	0.36m, NA	0.61m, 15.8 $^{\circ}$	0.22m, 4.02 $^{\circ}$	<b>0.19m</b> , <b>3.92<math>^{\circ}</math></b>	<b>0.19m</b> , 3.96 $^{\circ}$
Kitchen	0.23m, 5.35 $^{\circ}$	0.27m, 10.15 $^{\circ}$	0.37m, 8.83 $^{\circ}$	0.31m, NA	0.23m, 10.9 $^{\circ}$	0.23m, 4.93 $^{\circ}$	0.20m, 5.01 $^{\circ}$	<b>0.20m</b> , <b>4.94<math>^{\circ}</math></b>
Stairs	0.35m, 12.40 $^{\circ}$	0.29m, 12.46 $^{\circ}$	0.40m, 13.7 $^{\circ}$	<b>0.26m</b> , NA	0.26m, 21.3 $^{\circ}$	0.30m, 12.08 $^{\circ}$	0.30m, 13.37 $^{\circ}$	0.27m, <b>10.57<math>^{\circ}</math></b>
Average	0.23m, 8.12 $^{\circ}$	0.23m, 9.53 $^{\circ}$	0.31m, 9.85 $^{\circ}$	0.25m, NA	0.26m, 29.4 $^{\circ}$	0.21m, 7.77 $^{\circ}$	0.19m, 7.29 $^{\circ}$	<b>0.18m</b> , <b>6.55<math>^{\circ}</math></b>

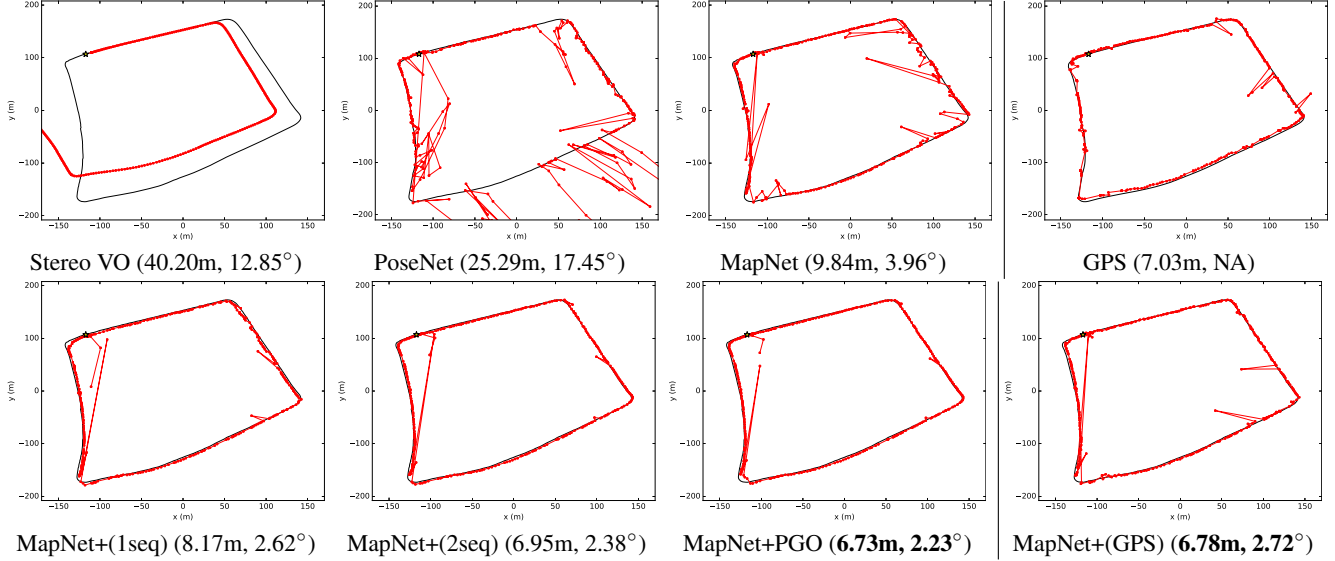


Figure 5: **Camera localization results on the LOOP scene (1120m long) of the Oxford RobotCar dataset [38].** The ground truth camera trajectory is the black line, the star indicates the first frame, and the red lines show the camera pose predictions. The caption of each figure shows the mean translation error (m) and mean rotation error ( $^{\circ}$ ). MapNet+(1seq) uses one unlabeled sequence, while MapNet+(2seq) uses two unlabeled sequences. **Left:** MapNet+ trained with unlabeled images and stereo VO. **Right:** MapNet+ trained with unlabeled images and GPS data.

their GPS locations, which are separate from the testing sequence. Since GPS measurements are sparse (less than 10% of images have corresponding GPS measurements), we first linearly interpolate GPS measurements for entire sequence. We define the loss of auxiliary data  $\mathcal{T}$  in Equation (5) as  $L_{\mathcal{T}}(\Theta) = \sum_{i=1}^{|\mathcal{T}|} h(\mathbf{p}_i, \hat{\mathbf{p}}_i)$ , where  $\hat{\mathbf{p}}_i$  is the linearly interpolated GPS measurement of the 2D camera location.

Figure 5 shows the estimated camera poses for all the methods in these two experiments along with the mean translation error (m) and rotation error ( $^{\circ}$ ). Figure 7 shows the cumulative distributions of the translation errors for all the methods on the LOOP route. In both figures, the left part shows that MapNet significantly improves the estimation compared to PoseNet and stereo VO. MapNet+ and MapNet+PGO further improve the pose predictions. The right part shows that by fusing GPS signals, MapNet+(GPS) obtains better results compared to MapNet and GPS alone.

**Results on the FULL Route** We also evaluated our approach on the challenging 9562 m long FULL route of the Oxford RobotCar dataset. Figure 6 shows the results of all the models with mean translation error (m) and rotation error ( $^{\circ}$ ). MapNet significantly outperforms the baseline PoseNet (both trained for 100 epochs) and the stereo VO (provided by the dataset). By fusing the stereo VO information, MapNet+ and MapNet+PGO further improve the result. The cumulative distributions of the translation errors also show the large improvement over the baselines.

Note that there are some outlier predictions in both LOOP (Fig. 5) and FULL (Fig. 6). These often correspond to images with large over-exposed regions, and can be filtered out with simple post-processing (e.g. temporal median filtering) as shown in the supplementary material. We also computed saliency maps  $s(x, y) = \frac{1}{6} \left| \sum_{i=1}^6 \frac{\partial p_i}{\partial I(x, y)} \right|$  (magnitude gradient of the mean of the 6-element output w.r.t. input image, maxed over the 3 color channels) for PoseNet

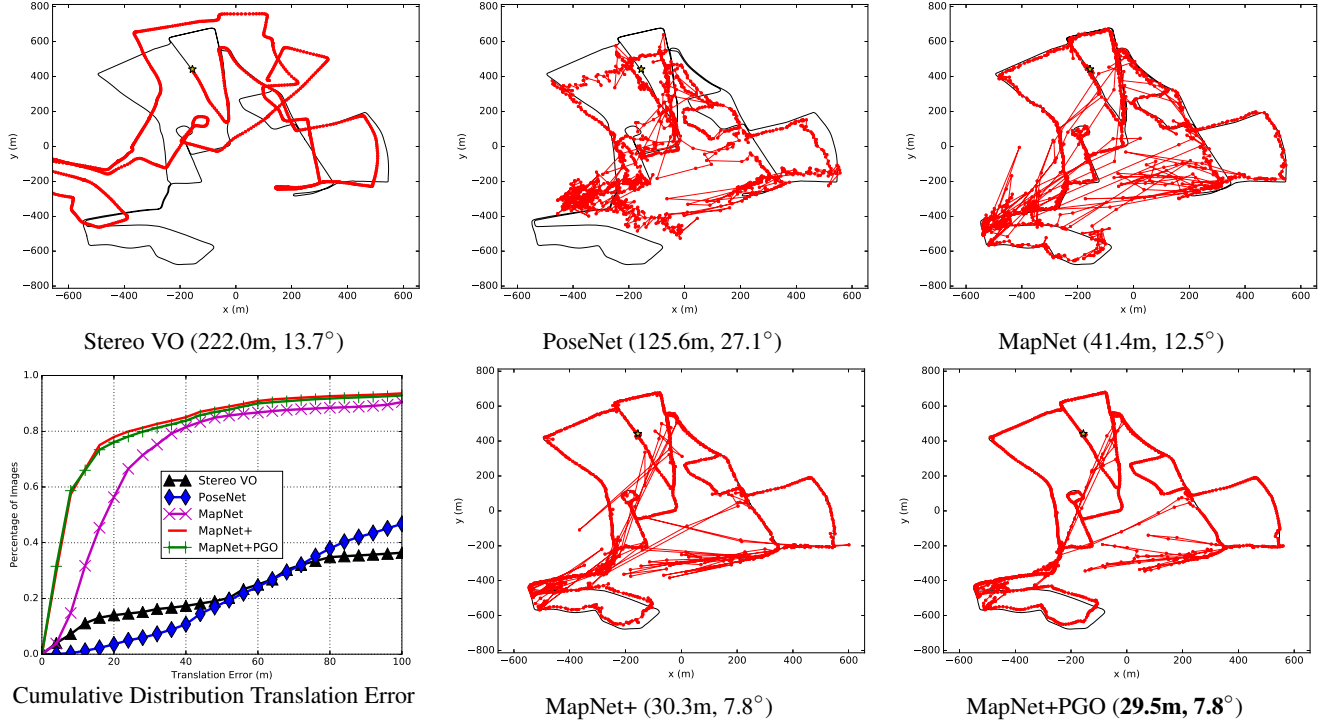


Figure 6: Comparison of camera localization results on the FULL scene (9562m long) of the Oxford RobotCar dataset [38]. The ground truth camera trajectory is the black line, and the star indicates the first frame. The red lines show the results of stereo VO (provided by the dataset), our version of PoseNet+log  $q$ , MapNet, and its variations. The caption of each figure shows the mean translation error (m) and mean rotation error ( $^{\circ}$ ). A plot of the cumulative distribution of the translation error is also included.

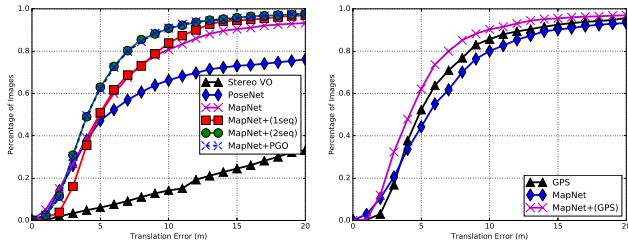


Figure 7: Cumulative distributions of the translation errors (m) for all the methods evaluated on Oxford RobotCar LOOP.  $x$ -axis is the translation error and  $y$ -axis is the percentage of frames with error less than the value.

and MapNet+ on both the 7-scenes and RobotCar dataset. We find that compared to PoseNet, MapNet+ focuses more on geometrically meaningful regions and its saliency map is more consistent over time. Examples are shown in the supplementary material.

## 5. Conclusions and Discussions

In summary, MapNet learns a *general, data-driven* map representation for camera localization. Our models bring geometric constraints widely used in visual SLAM and SfM into DNN-based learning, which allow us to learn from unlabeled data and to easily fuse other input sources (*e.g.*, vi-

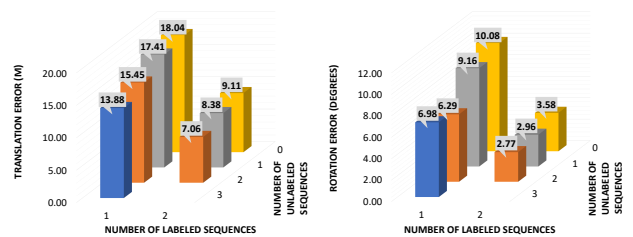


Figure 8: **Left:** Mean translation error (m) and **right:** mean rotation error ( $^{\circ}$ ) for MapNet+ models trained with varying amounts of labeled and unlabeled data on the Oxford RobotCar LOOP sequence. X-axis indicates the number of labeled sequences (1-2), Y-axis indicates the number of unlabeled sequences (0-3) and Z-axis indicates the error.

sual odometry, GPS, IMU). We evaluate our approach on both indoor and outdoor datasets and show significantly better performance than baselines.

Unlike the mapping in traditional visual SLAM systems, MapNet and MapNet+ cannot expand maps to unknown space. In future work, a tighter integration with visual SLAM systems may enable mapping of unknown regions. Leveraging the recent success in extracting high-level semantic information (*e.g.*, objects and scene composition) may also improve camera localization.



## References

- [1] PyTorch, 2017. **5**
- [2] S. Altmann. *Rotations, Quaternions, and Double Groups*. Dover Publications, 2005. **3**
- [3] R. Arandjelovic, P. Gronat, A. Torii, T. Pajdla, and J. Sivic. NetVLAD: CNN architecture for weakly supervised place recognition. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2016. **2**
- [4] R. Arandjelovic and A. Zisserman. All about VLAD. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2013. **2**
- [5] P. Bergmann, R. Wang, and D. Cremers. Online photometric calibration of auto exposure video for real-time visual odometry and slam. In *arXiv*, 2017. **2**
- [6] I. Borg and P. J. Groenen. *Modern multidimensional scaling: Theory and applications*. Springer Science & Business Media, 2005. **4**
- [7] E. Brachmann, A. Krull, S. Nowozin, J. Shotton, F. Michel, S. Gumhold, and C. Rother. DSAC: Differential RANSAC for camera localization. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2017. **2, 5**
- [8] L. Carlone, G. Calafiore, and F. Dellaert. Pose graph optimization in the complex domain: Duality, optimal solutions, and verification. *IEEE Transactions on Robotics*, 32(3):545–565, 2016. **1, 5**
- [9] O. Chapelle, B. Scholkopf, and A. Zien. *Semi-Supervised Learning*. MIT Press, 2006. **6**
- [10] J. Civera, D. Gaivez-Lopez, L. Riazuelo, J. Tardos, and J. Montiel. Towards semantic SLAM using a monocular camera. In *IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, 2011. **1, 2**
- [11] R. Clark, S. Wang, A. Markham, N. Trigoni, and H. Wen. VidLoc: A deep spatio-temporal model for 6-DoF video clip relocalization. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2017. **1, 2, 3, 5, 7**
- [12] M. Cummins and P. Newman. FAB-MAP: Probabilistic localization and mapping in the space of appearance. *The International Journal of Robotics Research*, 27(6):647–665, 2008. **1, 2**
- [13] E. B. Dam, M. Koch, and M. Lillholm. *Quaternions, interpolation and animation*, volume 2. 1998. **3**
- [14] A. J. Davison. Real-time simultaneous localisation and mapping with a single camera. In *Proceedings of IEEE International Conference on Computer Vision (ICCV)*, 2003. **2**
- [15] F. Dellaert and M. Kaess. Square Root SAM: Simultaneous localization and mapping via square root information smoothing. *Intl. J. of Robotics Research (IJRR)*, 25(12):1181–1204, Dec. 2006. **2**
- [16] O. Duchenne, J. Y. Audibert, R. Keriven, J. Ponce, and F. Segonne. Segmentation by transduction. In *2008 IEEE Conference on Computer Vision and Pattern Recognition*, pages 1–8, June 2008. **6**
- [17] T. Duckett, S. Marsland, and J. Shapiro. Fast, online learning of globally consistent maps. *Autonomous Robots*, 12(3):287–300, 2002. **1, 5**
- [18] J. Engel, V. Koltun, and D. Cremers. DSO: Direct sparse odometry. *IEEE Transactions on Pattern Analysis and Machine Intelligence (TPAMI)*, 2017. **1, 2, 4, 5, 6, 7**
- [19] J. Engel, T. Schops, and D. Cremers. Semi-dense visual odometry for a monocular camera. In *Proceedings of IEEE International Conference on Computer Vision (ICCV)*, 2013. **4**
- [20] J. Engel, T. Schops, and D. Cremers. LSD-SLAM: Large-scale direct monocular SLAM. In *Proceedings of European Conference on Computer Vision (ECCV)*, 2014. **1, 2**
- [21] R. Gomez-Ojeda, F.-A. Moreno, D. Scaramuzza, and J. Gonzalez-Jimenez. PL-SLAM: a Stereo SLAM System through the Combination of Points and Line Segments. *arXiv preprint arXiv:1705.09479*, 2017. **2**
- [22] V. Govindu. Combining two-view constraints for motion estimation. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2001. **1**
- [23] V. Govindu. Lie-algebraic averaging for globally consistent motion estimation. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2004. **1**
- [24] G. Grisetti, R. Kummerle, C. Stachniss, and W. Burgard. A tutorial on graph-based slam. *IEEE Intelligent Transportation Systems Magazine*, 2(4):31–43, 2010. **2, 5**
- [25] K. He, X. Zhang, S. Ren, and J. Sun. Deep residual learning for image recognition. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2016. **3**
- [26] D. Huynh. Metrics for 3D rotations: Comparison and analysis. *Journal of Mathematical Imaging and Vision*, 35(2):155–164, 2009. **3**
- [27] S. G. J. Stuhmer and D. Cremers. Real-time dense geometry from a handheld camera. In *Joint Pattern Recognition Symposium*, pages 11–20, 2010. **2**
- [28] H. Jegou, F. Perronnin, M. Douez, J. Sanchez, P. Perez, and C. Schmid. Aggregating local image descriptors into compact codes. *IEEE Transactions on Pattern Analysis and Machine Intelligence (TPAMI)*, 34(9):1704–1716, 2012. **2**
- [29] Y.-B. Jia. Quaternion and Rotation. Com S 477/577 Lecture Notes at <http://web.cs.iastate.edu/~cs577/handouts/quaternion.pdf>, 2008. **3**
- [30] A. Kendall and R. Cipolla. Modeling uncertainty in deep learning for camera relocalization. In *IEEE International Conference on Robotics and Automation (ICRA)*, 2016. **1, 2, 3, 5, 6**
- [31] A. Kendall and R. Cipolla. Geometric loss functions for camera pose regression with deep learning. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2017. **1, 2, 3, 4, 5, 6, 7**
- [32] A. Kendall, M. Grimes, and R. Cipolla. PoseNet: A convolutional network for real-time 6-DOF camera relocalization. In *Proceedings of IEEE International Conference on Computer Vision (ICCV)*, 2015. **1, 2, 3, 5, 6**
- [33] D. Kingma and J. Ba. Adam: A method for stochastic optimization. *arXiv preprint arXiv:1412.6980*, 2014. **5**
- [34] G. Klein and D. Murray. Parallel tracking and mapping for small AR workspaces. In *IEEE and ACM International Symposium on Mixed and Augmented Reality (ISMAR)*, 2007. **1, 2**

- [35] Y. Li, N. Snavely, D. Huttenlocher, and P. Fua. Worldwide pose estimation using 3D point clouds. In *Proceedings of European Conference on Computer Vision (ECCV)*, 2012. 1, 2
- [36] M. A. Lourakis and A. Argyros. SBA: A Software Package for Generic Sparse Bundle Adjustment. *ACM Trans. Math. Software*, 36(1):1–30, 2009. 2
- [37] F. Lu and E. Milios. Globally consistent range scan alignment for environment mapping. *Autonomous Robots*, pages 334–349, 1997. 1, 2, 5
- [38] W. Maddern, G. Pascoe, C. Linegar, and P. Newman. 1 Year, 1000km: The Oxford RobotCar Dataset. *The International Journal of Robotics Research (IJRR)*, 36(1):3–15, 2017. 1, 2, 4, 5, 7, 8
- [39] D. Martinec and T. Pajdla. Robust rotation and translation estimation in multiview reconstruction. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2007. 1
- [40] I. Melekhov, J. Ylioinas, J. Kannala, and E. Rahtu. Image-based localization using hourglass networks. *arXiv*, abs/1703.07971, 2017. 1, 2, 3, 5, 7
- [41] M. Montemerlo, S. Thrun, D. Koller, and B. Wegbreit. FastSLAM: A factored solution to the simultaneous localization and mapping problem. In *Eighteenth National Conference on Artificial Intelligence*, pages 593–598, 2002. 2
- [42] R. Mur-Artal, J. M. M. Montiel, and J. D. Tardós. ORB-SLAM: a versatile and accurate monocular SLAM system. *CoRR*, abs/1502.00956, 2015. 1, 2
- [43] R. A. Newcombe, S. J. Lovegrove, and A. J. Davison. DTAM: Dense tracking and mapping in real-time. In *Proceedings of IEEE International Conference on Computer Vision (ICCV)*, pages 2320–2327, 2011. 1, 2
- [44] D. Nistér, O. Naroditsky, and J. Bergen. Visual odometry. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, pages 652–659, 2004. 4
- [45] R. Salas-Moreno, R. Newcombe, H. Strasdat, and P. Kelly. SLAM++: Simultaneous localization and mapping at the level of objects. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2013. 1, 2
- [46] T. Sattler, B. Leibe, and L. Kobbelt. Fast image-based localization using direct 2d-3d matching. In *Proceedings of IEEE International Conference on Computer Vision (ICCV)*, 2011. 1, 2
- [47] T. Sattler, B. Leibe, and L. Kobbelt. Efficient and effective prioritized matching for large-scale image-based localization. *IEEE Transactions on Pattern Analysis and Machine Intelligence (TPAMI)*, 39(9):1744–1756, 2017. 1, 2
- [48] J. Shotton, B. Glocker, C. Zach, S. Izadi, A. Criminisi, and A. Fitzgibbon. Scene coordinate regression forests for camera relocalization in RGBD images. In *Proceedings of IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2013. 1, 2, 5, 6, 7
- [49] H. Strasdat, J. M. M. Montiel, and A. J. Davison. Visual SLAM: Why filter? *Image Vision Computing*, 30(2):65–77, Feb. 2012. 2
- [50] H. Su, C. Qi, Y. Li, and L. Guibas. Render for CNN: Viewpoint estimation in images using CNNs trained with rendered 3D model views. In *Proceedings of IEEE International Conference on Computer Vision (ICCV)*, 2015. 3
- [51] Y. Taguchi, Y.-D. Jian, S. Ramalingam, and C. Feng. Point-plane SLAM for hand-held 3d sensors. In *IEEE International Conference on Robotics and Automation (ICRA)*, pages 5182–5189, 2013. 2
- [52] S. Thrun. Robotic mapping: A survey. In G. Lakemeyer and B. Nebel, editors, *Exploring Artificial Intelligence in the New Millenium*. Morgan Kaufmann, 2002. 2
- [53] S. Thrun and M. Montemerlo. The GraphSLAM algorithm with applications to large-scale mapping of urban structures. *International Journal on Robotics Research*, 25(5/6):403–430, 2005. 2
- [54] B. Triggs, P. F. McLauchlan, R. I. Hartley, and A. W. Fitzgibbon. Bundle adjustment - a modern synthesis. In *Proceedings of the International Workshop on Vision Algorithms: Theory and Practice*, ICCV '99, pages 298–372, 2000. 2
- [55] F. Walch, C. Hazirbas, L. Leal-Taixe, T. Sattler, S. Hilsenbeck, and D. Cremers. Image-based localization using LSTMs for structured feature correlation. In *Proceedings of IEEE International Conference on Computer Vision (ICCV)*, 2017. 1, 2, 3, 5, 7
- [56] H. Zhou, D. Zou, L. Pei, R. Ying, P. Liu, and W. Yu. StructSLAM: Visual SLAM with building structure lines. *IEEE Transactions on Vehicular Technology*, 64(4):1364–1375, 2015. 1